Please check the examination details below	w before entering your candidate information
Candidate surname	Other names
Pearson Edexcel Level 3 GCE	tre Number Candidate Number
Friday 22 May 2	.020
Afternoon (Time: 1 hour 30 minutes)	Paper Reference 9FM0/3A
Further Mathemate Advanced Paper 3A: Further Pure Materials	
You must have: Mathematical Formulae and Statistical	l Tables (Green), calculator

Candidates may use any calculator permitted by Pearson regulations.
Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶







1 Han PHanital's Dula to	ala avv. 4la a4			
1. Use l'Hospital's Rule to	snow that			
	1: (e ^s	$\frac{\sin x - \cos(3x) - e}{\tan(2x)}$) 3	
	IIII —	tan(2r)	$- = -\frac{1}{2}$	
	$X \rightarrow {2}$	tan(2x)	2	
				(5)
				(5)

Question 1 continued	
(Total for Question 1 is 5 m	arks)



(6)

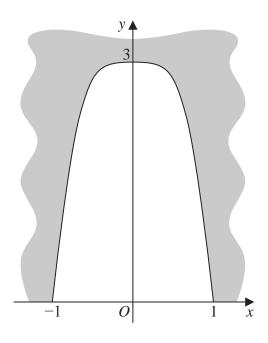


Figure 1

Figure 1 shows a sketch of the vertical cross-section of the entrance to a tunnel. The width at the base of the tunnel entrance is 2 metres and its maximum height is 3 metres.

The shape of the cross-section can be modelled by the curve with equation y = f(x) where

$$f(x) = 3\cos\left(\frac{\pi}{2}x^2\right) \qquad x \in [-1, 1]$$

A wooden door of uniform thickness 85 mm is to be made to seal the tunnel entrance.

Use Simpson's rule with 6 intervals to estimate the volume of wood required for this door, giving your answer in m³ to 4 significant figures.

Question 2 continued	
('Tot	al for Question 2 is 6 marks)



- 3. The points A, B and C, with position vectors $\mathbf{a} = 3\mathbf{i} 2\mathbf{j} + \mathbf{k}$, $\mathbf{b} = \mathbf{i} + 4\mathbf{j} + 5\mathbf{k}$ and $\mathbf{c} = -2\mathbf{i} + 3\mathbf{j} + 3\mathbf{k}$ respectively, lie on the plane Π
 - (a) Find $\overrightarrow{AB} \times \overrightarrow{AC}$

(3)

(b) Find an equation for Π in the form $\mathbf{r}.\mathbf{n} = p$

(2)

The point *D* has position vector $8\mathbf{i} + 7\mathbf{j} + 5\mathbf{k}$

(c) Determine the volume of the tetrahedron ABCD

(4)

Question 3 continued	



Question 3 continued

Question 3 continued	
	(Total for Question 3 is 9 marks)



4.

$$f(x) = x^4 \sin(2x)$$

Use Leibnitz's theorem to show that the coefficient of $(x - \pi)^8$ in the Taylor series expansion of f(x) about π is

$$\frac{a\pi + b\pi^3}{315}$$

where a and b are integers to be determined.

(8)

$$\begin{bmatrix} The \ Taylor \ series \ expansion \ of \ f(x) \ about \ x = k \ is \ given \ by \\ f(x) = f(k) + (x - k)f'(k) + \frac{(x - k)^2}{2!} f''(k) + \dots + \frac{(x - k)^r}{r!} f^{(r)}(k) + \dots \end{bmatrix}$$

Question 4 continued	
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Question 4 continued

Question 4 continued	
	(Total for Question 4 is 8 marks)



5. The ellipse E has equation

$$\frac{x^2}{36} + \frac{y^2}{16} = 1$$

The points S and S' are the foci of E.

(a) Find the coordinates of S and S'

(3)

(b) Show that for any point *P* on *E*, the triangle *PSS'* has constant perimeter and determine its value.

(4)

Question 5 continued	
(То	tal for Question 5 is 7 marks)



6. A physics student is studying the movement of particles in an electric field. In one experiment, the distances in micrometres of two moving particles, A and B, from a fixed point O are modelled by

$$d_{A} = |5t - 31|$$
$$d_{B} = |3t^{2} - 25t + 8|$$

respectively, where t is the time in seconds after motion begins.

(a) Use algebra to find the range of time for which particle A is further away from O than particle B is from O.

(8)

It was recorded that the distance of particle *B* from *O* was less than the distance of particle *A* from *O* for approximately 4 seconds.

(b) Use this information to assess the validity of the model.

(2)

Question 6 continued	



Question 6 continued

Question 6 continued
(Total for Question 6 is 10 marks)



7. The points $P(9p^2, 18p)$ and $Q(9q^2, 18q)$, $p \neq q$, lie on the parabola C with equation

$$y^2 = 36x$$

The line l passes through the points P and Q

(a) Show that an equation for the line l is

$$(p+q)y = 2(x+9pq)$$
 (3)

The normal to C at P and the normal to C at Q meet at the point A.

(b) Show that the coordinates of A are

$$(9(p^2+q^2+pq+2), -9pq(p+q))$$
(7)

Given that the points P and Q vary such that l always passes through the point (12, 0)

(c) find, in the form $y^2 = f(x)$, an equation for the locus of A, giving f(x) in simplest form.

Question 7 continued



Question 7 continued

Question 7 continued	
(To	otal for Question 7 is 14 marks)



$$f(x) = \frac{3}{13 + 6\sin x - 5\cos x}$$

Using the substitution $t = \tan\left(\frac{x}{2}\right)$

(a) show that f(x) can be written in the form

$$\frac{3(1+t^2)}{2(3t+1)^2+6}$$

(3)

(b) Hence solve, for $0 < x < 2\pi$, the equation

$$f(x) = \frac{3}{7}$$

giving your answers to 2 decimal places where appropriate.

(5)

(c) Use the result of part (a) to show that

$$\int_{\frac{\pi}{3}}^{\frac{4\pi}{3}} f(x) dx = K \left(\arctan\left(\frac{\sqrt{3} - 9}{3}\right) - \arctan\left(\frac{\sqrt{3} + 3}{3}\right) + \pi \right)$$

where K is a constant to be determined.

(8)



Question 8 continued	



Question 8 continued

Question 8 continued	



Question 8 continued
(Total for Question 8 is 16 marks)
TOTAL FOR PAPER IS 75 MARKS

